



We recognize and acknowledge that McMaster University meets and learns on the traditional territories of the Mississauga and Haudenosaunee nations, and within the lands protected by the "Dish With One Spoon" wampum, an agreement amongst all allied Nations to peaceably share and care for the resources around the Great Lakes.

MATH 4AT3 – Topics in Analysis: Distribution Theory and Fourier Analysis Syllabus 2022 WinterTerm

Instructor: Prof. L. Bronsard | E-mail: bronsard@mcmaster.ca | Office: HH-424 | Office Hours: TBA | Ext: x23418

Website: TBA

Note: This is a tentative version of the course outline. Note that this course will NOT be listed on Avenue to Learn, but will be accessed via Microsoft Teams if we teach online.

COURSE DESCRIPTION AND OBJECTIVES

Math 4AT3 -- Topics in Analysis (Winter 2022) Distributions and Fourier transforms Instructor: Dr. Bronsard <u>bronsard@mcmaster.ca</u>

Analysis is the field of mathematics which developed from calculus and its applications. While it forms part of pure mathematics, analysis plays an essential role in many important applied fields. The main themes of this course will be the Theory of Distributions, Fourier Analysis, with applications to Partial Differential Equations. The specific applications covered will depend on the interest of the class. The primary book I plan to use is "A Guide to Distribution Theory and the Fourier Transform", by Robert Strichartz, World Scientific Publishing Company.

Distribution theory was one of the two great revolutions in mathematical analysis in the 20th century, the other being Lebesgue integration theory. Distribution theory can be thought of as the completion of differential calculus, while Lebesgue theory is that of integral calculus. We will learn the ideas that underline the techniques from Distribution theory and use these techniques in Fourier analysis and applications in PDE's.

The evaluation will depend on the size of the class. There could be one Midterm, and either a Final exam or a Takehome exam (which could include a presentation.) There will be 4-5 written assignments, possibly given via Kritik.

The only prerequisite for this class is Math 3IA3, with a grade of at least B. There is no need to know any PDE's for this class.

Calendar description: Precise topics will vary; consult the department for current information. Possible topics include: functional analysis, measure theory, harmonic analysis, calculus of variations, theory of distributions.

Three lecture; one term Prerequisite(s): Math 3IA3

Course Objectives:



Students will be expected to:

- To use their knowledge from analysis and calculus to learn enough of the basics from Distribution theory and Fourier analysis to be able to understand interesting natural phenomenon via examples. This class is expected to be enjoyable as it is putting together many of the concepts that you have learned in previous classes to learn new concepts.
- to learn precise statements of definitions and theorems presented in class, their proofs, and to recognize when they apply (and when they don't!) and use them.
- to develop critical thinking and feedback delivery skills.

Topics

Topics will include: the theory of Distributions, Fourier analysis and applications to PDE's

• This is meant as a general outline of topics which I intend to cover. The actual material may differ according to the pace of the course, and other topics may be introduced along the way.

Lectures

All lectures will be given likely in person, but otherwise on-line via Teams, during the scheduled time slot:

• MoTh 3:30PM - 4:20PM and Tu 4:30-5:20.

While my preference is for all of the course to be presented live, technical and pedagogical issues may make this unfeasible, and some parts of the course may be given as recorded video lectures or in the form of reading assignments. You are responsible for all content, whether delivered via live video streaming, video recordings, or in written form.

Communication

Online delivery of lecture material will be done using Microsoft Teams. Important information will be communicated using the course web page (TBA)

Tests and the Final Exam will likely be submitted using Crowdmark. Assignments/Activities may be evaluated through Kritik. *This course will not be listed on Avenue to Learn.*

Tutorials

There is no tutorials for this class.

MATERIALS & FEES

MATERIALS/ RESOURCES

- A Guide to Distribution Theory and the Fourier Transform", by Robert Strichartz, World Scientific Publishing Company *is strongly recommended*
- The course will cover at least material selected from chapters 1-5
- <u>Kritik</u> (depending on the size of the class): Kritik is an on-line platform for submission and evaluation of assignments/activities. Each activity includes three separate phases. First, you submit your solution/material as a scan/powerpoint to your Kritik account. Then, you will be asked to anonymously evaluate a certain number (4 or 5) of other students' solutions/material. Finally, you will receive the other students' evaluations of your submission, and make an evaluation of the utility of their comments. Kritik, if required, will be provided for this

class. If the classes uses Kritik, you should receive an email with an invitation to create a Kritik account for this course; if you do not receive one, please contact me via email.

In case of VIRTUAL COURSE DELIVERY

To follow and participate in virtual classes it is expected that you have reliable access to the following:

- A computer that meets performance requirements <u>found here</u>.
- An internet connection that is fast enough to stream video.
- Computer accessories that enable class participation, such as a microphone, speakers and webcam when needed.

If you think that you will not be able to meet these requirements, please contract <u>uts@mcmaster.ca</u> as soon as you can. Please visit the <u>Technology Resources for Students page</u> for detailed requirements. If you use assistive technology or believe that our platforms might be a barrier to participating, please contact <u>Student Accessibility</u> <u>Services</u>, <u>sas@mcmaster.ca</u>, for support.

****Note 1:** All course information will be posted on the course webpage

TBA

You are expected to check the webpage often, at least before each lecture (if you think you will not be able to do it, talk to your instructor as soon as possible).

COURSE OVERVIEW AND ASSESSMENT

Assignments/Activities and Practice Problems

If there is enough students in the class, Assignments/Activities will be submitted through Kritik, as described above. There will be about 4 assignments/activities, scheduled approx. every two/three weeks. Additional weekly practice problems will be announced on the course. The practice problems are essential for your understanding, but will not be collected and will not count towards your homework grade. You will be responsible for their content on the test and final exam.

EVALUATION – Marking Scheme: two options depending on the class size:

This will be made definite before class starts and will depend on the class size: if the class is big enough it will be

As	sessment	Weight
\checkmark	ONE Midterm Test (30%)	30%
\checkmark	Final Examination	40%
\checkmark	Kritik	30%

If the class is smaller, it will be 60% on assignements and 40% on the Final evaluation.

Alternative marking schemes may also be used, in which case your final grade will be given by the maximum mark obtained among all schemes considered.

Midterm Tests



There might be ONE midterm test held during regular class time that will be likely submitted through Crowdmark.

Final Exam

A 2 hrs final examination may be given using Crowdmark which would cover all course material. The date and time will be announced sometime later in the term.

REQUESTS FOR RELIEF FOR MISSED ACADEMIC TERM WORK

<u>McMaster Student Absence Form (MSAF)</u>: In the event of an absence for medical or other reasons, students should review and follow the Academic Regulation in the Undergraduate Calendar "Requests for Relief for Missed Academic Term Work".

ACADEMIC ACCOMMODATION OF STUDENTS WITH DISABILITIES

Students with disabilities who require academic accommodation must contact <u>Student Accessibility Services (SAS</u>) at 905-525-9140 ext. 28652 or <u>sas@mcmaster.ca</u> to make arrangements with a Program Coordinator. For further information, consult McMaster University's <u>Academic Accommodation of Students with Disabilities</u> policy.

ACADEMIC ACCOMMODATION FOR RELIGIOUS, INDIGENOUS OR SPIRITUAL OBSERVANCES (RISO)

Students requiring academic accommodation based on religious, indigenous or spiritual observances should follow the procedures set out in the <u>RISO</u> policy. Students should submit their request to their Faculty Office *normally within 10 working days* of the beginning of term in which they anticipate a need for accommodation or to the Registrar's Office prior to their examinations. Students should also contact their instructors as soon as possible to make alternative arrangements for classes, assignments, and tests.

COURSES WITH AN ON-LINE ELEMENT

Some courses may use on-line elements (e.g. e-mail, Avenue to Learn (A2L), LearnLink, web pages, capa, Moodle, ThinkingCap, etc.). Students should be aware that, when they access the electronic components of a course using these elements, private information such as first and last names, user names for the McMaster e-mail accounts, and program affiliation may become apparent to all other students in the same course. The available information is dependent on the technology used. Continuation in a course that uses on-line elements will be deemed consent to this disclosure. If you have any questions or concerns about such disclosure, please discuss this with the course instructor.

ONLINE PROCTORING

Some courses may use online proctoring software for tests and exams. This software may require students to turn on their video camera, present identification, monitor and record their computer activities, and/or lock/restrict their browser or other applications/software during tests or exams. This software may be required to be installed before the test/exam begins.

ACADEMIC INTEGRITY

You are expected to exhibit honesty and use ethical behaviour in all aspects of the learning process. Academic credentials you earn are rooted in principles of honesty and academic integrity.

It is your responsibility to understand what constitutes academic dishonesty.

Academic dishonesty is to knowingly act or fail to act in a way that results or could result in unearned academic credit or advantage. This behaviour can result in serious consequences, e.g. the grade of zero on an assignment, loss

of credit with a notation on the transcript (notation reads: "Grade of F assigned for academic dishonesty"), and/or suspension or expulsion from the university. For information on the various types of academic dishonesty please refer to the <u>Academic Integrity Policy</u>, located at <u>https://secretariat.mcmaster.ca/university-policies-procedures-guidelines/</u>

The following illustrates only three forms of academic dishonesty:

- plagiarism, e.g. the submission of work that is not one's own or for which other credit has been obtained.
- improper collaboration in group work.
- copying or using unauthorized aids in tests and examinations.

AUTHENTICITY / PLAGIARISM DETECTION

Some courses may use a web-based service (Turnitin.com) to reveal authenticity and ownership of student submitted work. For courses using such software, students will be expected to submit their work electronically either directly to Turnitin.com or via an online learning platform (e.g. A2L, etc.) using plagiarism detection (a service supported by Turnitin.com) so it can be checked for academic dishonesty.

Students who do not wish their work to be submitted through the plagiarism detection software must inform the Instructor before the assignment is due. No penalty will be assigned to a student who does not submit work to the plagiarism detection software. **All submitted work is subject to normal verification that standards of academic integrity have been upheld** (e.g., on-line search, other software, etc.). For more details about McMaster's use of Turnitin.com please go to <u>www.mcmaster.ca/academicintegrity</u>.

CONDUCT EXPECTATIONS

As a McMaster student, you have the right to experience, and the responsibility to demonstrate, respectful and dignified interactions within all our living, learning and working communities. These expectations are described in the <u>Code of Student Rights & Responsibilities (the "Code")</u>. All students share the responsibility of maintaining a positive environment for the academic and personal growth of all McMaster community members, whether in person or online.

It is essential that students be mindful of their interactions online, as the Code remains in effect in virtual learning environments. The Code applies to any interactions that adversely affect, disrupt, or interfere with reasonable participation in University activities. Student disruptions or behaviours that interfere with university functions on online platforms (e.g. use of Avenue 2 Learn, WebEx or Zoom for delivery), will be taken very seriously and will be investigated. Outcomes may include restriction or removal of the involved students' access to these platforms.

COPYRIGHT AND RECORDING

Students are advised that lectures, demonstrations, performances, and any other course material provided by an instructor include copyright protected works. The Copyright Act and copyright law protect every original literary, dramatic, musical and artistic work, **including lectures** by University instructors.

The recording of lectures, tutorials, or other methods of instruction may occur during a course. Recording may be done by either the instructor for the purpose of authorized distribution, or by a student for the purpose of personal study. Students should be aware that their voice and/or image may be recorded by others during the class. Please speak with the instructor if this is a concern for you.

RESEARCH ETHICS – NA



EXTREME CIRCUMSTANCES

The University reserves the right to change the dates and deadlines for any or all courses in extreme circumstances (e.g., severe weather, labour disruptions, etc.). Changes will be communicated through regular McMaster communication channels, such as McMaster Daily News, A2L and/or McMaster email.

Disclaimer

The instructor and university reserve the right to modify elements of the course during the term. The university may change the dates and deadlines for any or all courses in extreme circumstances. If either type of modification becomes necessary, reasonable notice and communication with the students will be given with explanation and the opportunity to comment on changes. It is the responsibility of students to check their McMaster email and course websites weekly during the term and to note any changes. Announcements will be made in class and by using the course email distribution list."